

7 - Recursion

Sunday, 9 August 2026 14:30

A function that repeatedly calls itself.

eg: Factorial

$$n! = n (n-1) (n-2) \dots (1)$$

$$\Rightarrow n! = n (n-1)!$$

$$\Rightarrow \text{fact}(n) = n \cdot \text{fact}(n-1)$$

```
recursion/factorial.c
1  #include <stdio.h>
2
3  int fact(int n){
4      if (n==1 || n==0){
5          return 1;
6      }else{
7          return (n * fact(n-1));
8      }
9  }
10
11 int main(){
12     int n = 5;
13     printf("%d", fact(n));
14     return 0;
15 }
16
```

```
recursion - zsh
(base) arneshbanerjee@Arneshs-MacBook-Air recursion % gcc factorial.c
(base) arneshbanerjee@Arneshs-MacBook-Air recursion % ./a.out
120%
(base) arneshbanerjee@Arneshs-MacBook-Air recursion %
```

Visual Rep

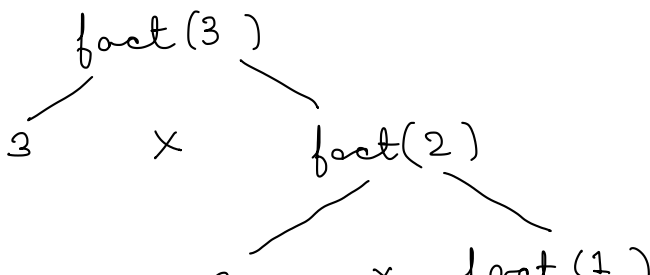
$$f(5) = 5 \times f(4) = 5 \times 24 = \underline{120}$$

$$f(4) = 4 \times f(3) = 4 \times 6 = \underline{24}$$

$$f(3) = 3 \times f(2) = 3 \times 2 = \underline{6}$$

$$f(2) = 2 \times f(1) = 2 \times 1 = \underline{2}$$

$$f(1) = 1 \text{ (defined in if)}$$



2 1 0 1

↓

1

Questions

(i)

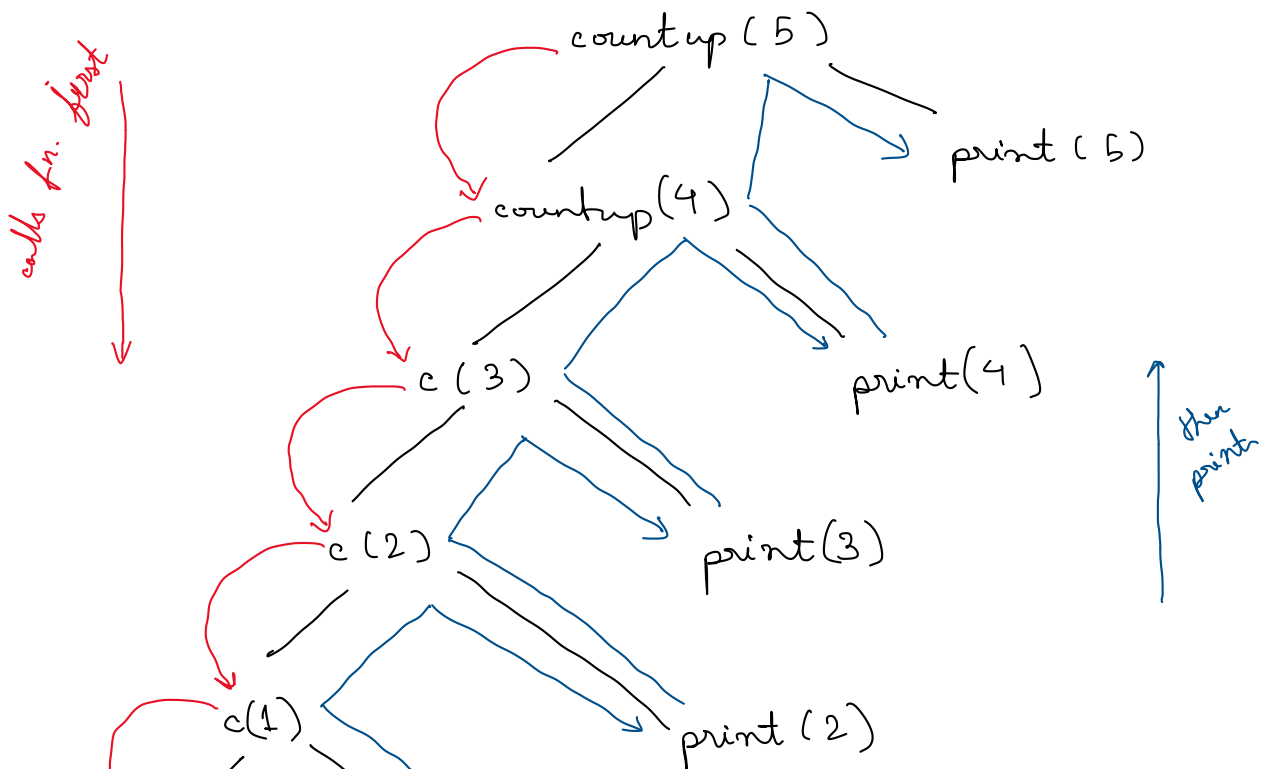
```
recursion/countup.c: void countup( )
1  #include<stdio.h>
2
3  void countup(int n){
4      if(n==0){
5          return;
6      }
7      countup(n-1);
8      printf("%d", n);
9  }
10
11
12 int main(){
13     countup(5);
14     return 0;
15 }
16
```

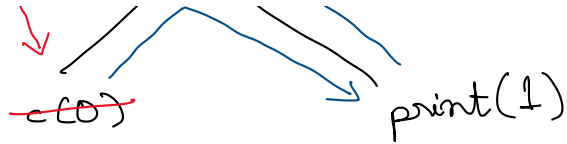
```
(base) arneshbanerjee@Arneshs-MacBook-Air recursion % gcc countup.c
(base) arneshbanerjee@Arneshs-MacBook-Air recursion % ./a.out
12345
(base) arneshbanerjee@Arneshs-MacBook-Air recursion %
```

The recursion gets called first & then print.

So the print only happens once all the recursions are over

And since last countup(0) finishes first, the countup(1) print happens first.





o/p: 1 2 3 4 5

ii

```

1  #include<stdio.h>
2
3  void func(){
4      static int n = 5;
5
6      if (n==0)
7          return;
8      n--;
9      func();
10     printf("%d ", n);
11
12 }
13
14
15 int main()
16 {
17     func();
18 }

```

o/p → 0 0 0 0 0

∴ at last step
n = 0.

And since n is
a static variable.

So n = 0 persists for
all print values.

iii

```

int recursiveFunc(int n)
{
    static int count = 0;

    if (n <= 0)
        return count;

    count++;
}

```

$\text{rF}(5)$
 $/$
 $\text{rF}(4)$
 $/$
 $\text{rF}(3)$
 $/$

```

    return recursiveFunc(n - 1);
}

int main()
{
    int result = recursiveFunc(5);
    printf("Result: %d\n", result);
}

```

$\nearrow f(2)$
 $\swarrow$
 $\nearrow f(1)$
 $\swarrow$
 $\nearrow f(0)$

5

iv

```

int recursiveFunc(int n)
{
    static int count = 0;

    if (n <= 0)
        return count;

    count += n;
    return recursiveFunc(n - 1);
}

int main()
{
    int result = recursiveFunc(3);
    printf("Result: %d\n", result);
}

```

$\nearrow f(3)$ $c = 3$
 $\swarrow$
 $\nearrow f(2)$ $c = 5$
 $\swarrow$
 $\nearrow f(1)$ $c = 6$
 $\swarrow$
 $\nearrow f(0)$ $c = 6$
 $\downarrow$
 returns count

v

```

void fun(int n)
{
    if (n == 0) return;
    else {
        fun(n--);
        printf("%d ", n);
    }
}

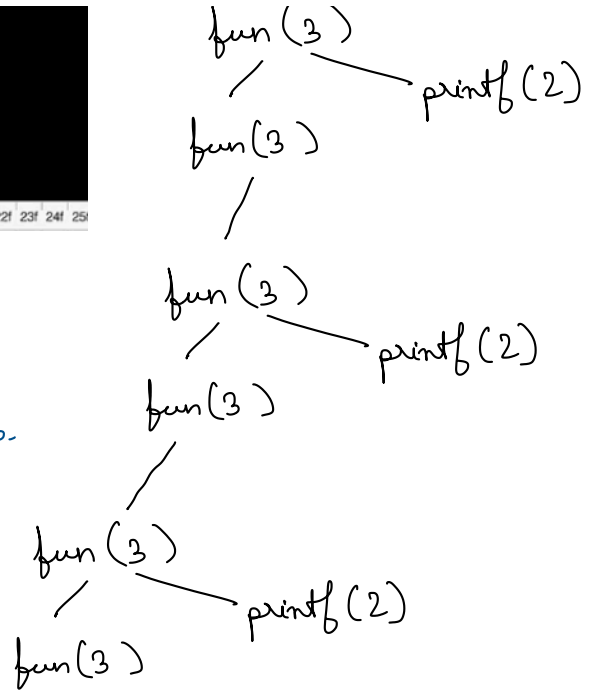
```

Starts with
fun(3)

→ fun(3) gets passed again since it's post decrement operator

```
main()  
{  
    fun(3);  
}
```

So this runs infinitely & results in stack overflow.



vi

```
#include <stdio.h>
void func2(int n); // Forward declaration
void func1(int n)
{
    if (n > 0)
    {
        printf("func1: %d\n", n);
        func2(n - 1);
    }
}

void func2(int n)
{
    if (n > 0)
    {
        printf("func2: %d\n", n);
        func1(n - 1);
    }
}

int main()
{
    func1(3);
    return 0;
}
```

func 1: 3
func 2: 2
func 1: 1

(vi) Gate CSE 2004

```
int f(int n)
{
    static int i = 1;
```

$$n=1, i=1 \rightarrow n=2, i=2$$
$$0 \quad | \quad f(n) = n^2 - n + 2 \rightarrow n^2 - n + 2$$

```

if(n >= 5) return n;
n = n+i;
i++;
return f(n);
}

```

$f(4) \Rightarrow n=4, i=3 \rightarrow n=7$

$\downarrow$
return(n)

Ans) 7

Q: What will be value returned by $f(1)$.

vii

```

int f(int n)
{
    static int r = 0;
    if (n <= 0) return 1;
    if (n > 3)
    {
        r = n;
        return f(n-2) + 2;
    }
    return f(n-1) + r;
}

```

What is the value of $f(5)$?

A. 5
B. 7
C. 9
D. 18

$f(5)$ ($n=5, r=5$)

$f(3) + 2 \rightarrow 18$ - Ans

$f(2) + 5 \rightarrow 16$

$f(1) + 5 \rightarrow 11$

$f(0) + 5 = 6$

1

vi

```
void count (int n) {
    static int d=1;

    printf ("%d",n);
    printf ("%d",d);
    d++;
    if (n>1) count (n-1);
    printf ("%d",d);
}

void main(){
    count (3);
}
```

A. 312213444
 B. 312111222
 C. 3122134
 D. 3121112

3 1 2 2 1 3 4 4 4

ix

Gate CS 2017

Consider the following two functions.

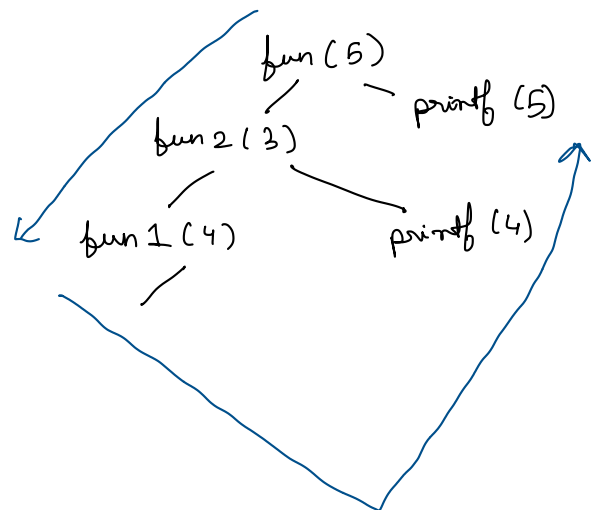
```
void fun1(int n) {
    if(n == 0) return;
    printf("%d", n);
    fun2(n - 2);
    printf("%d", n);
}

void fun2(int n) {
    if(n == 0) return;
    printf("%d", n);
    fun1(++n);
    printf("%d", n);
}
```

The output printed when fun1(5) is called is

A. 53423122233445
 B. 53423120112233
 C. 53423122132435

5 3 4 2 3 1 2 2 2 3 3 4 4 5



So, last 2 digits are '45'

So answer is (A)